Flexible and Robust Peat core age modeling controlling accumulation rates to asses integrated precision using radiocarbon dating

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Christen/Blaauw ()

- Building a chronology, ie. a relationship between age and depth, of any (peat, lake) core in paleo-studies is crucial, to match and test the synchronicity of events across sites, "leads and lags", etc.
- Radiocarbon dating (and other dating methods) are used to make a chronology.
- Prior information about accumulation rates is available.
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Bpeat: What we can do

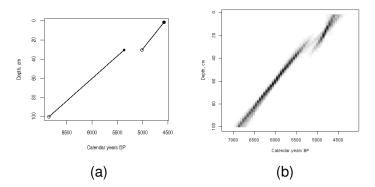


Figure: MSB2K peat core (a) piece-wise linear chronology, (b) uncertainty to the piece wise linear model.

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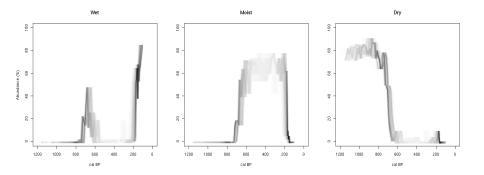


Figure: Proxy distribution including chronological error assessment.

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- Robust output, considering outliers, etc.
- Robust numerical calculations.
- User friendly software, although NO plug-click-and-play: Bacon.

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We have a series of radiocarbon determinations $y_j \pm \sigma_j$; j = 1, 2, ..., m taken along a (peat, lake, etc.) core at depths d_j . A semiparametric model is proposed to establish a relationship between the (unknown) age of peat and depth, d,

$$G(d,\theta,x) = \theta + \sum_{j=1}^{i} x_j \Delta c + x_{i+1}(d-c_i);$$

where $c_i \leq d < c_{i+1}$, i < K, and $c_0 < c_1 < \cdots < c_K$ are depths uniformly spaced along the peat core with difference Δc and $x = (x_1, x_2, \dots, x_K)$.

- That is, the core is divided into *K* equally spaced sections and *x_j* is the accumulation rate of section *j*.
- We include a coherence behaviour on the accumulation rates: $x_j = wx_{j+1} + (1 - w)\alpha_j.$
- $w \in [0, 1]$ and $\alpha_j \sim Gamma(a_\alpha, b_\alpha)$ iid, with a_α and b_α known.

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- A robust, novel, model for radiocarbn determinations is used, that protects the chronology against **outliers**. (Christen, J.A. y Pérez E., S. (2009), "A new robust statistical model for radiocarbon data", *Radiocarbon*, **51**(3) (to appear)).
- A new improved numerical technique is used (reduced time calculations from hours to minutes).

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Bacon chronologies

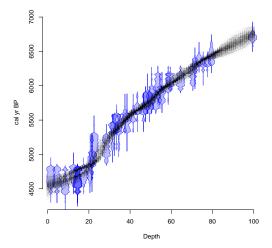


Figure: Bacon MSB2K chronology.

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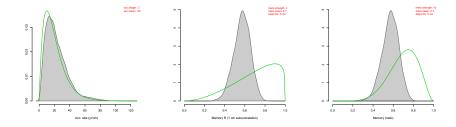


Figure: Bacon MSB2K analysis: prior (green) and posterior distributions for the tuning parameters.

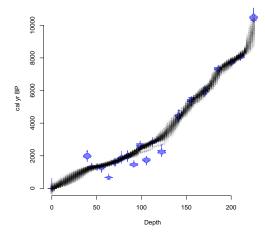


Figure: Bacon RLGH3 chronology, lake core.

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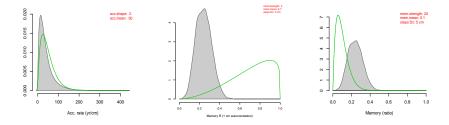


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¡Gracias!

